

CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge Ordinary Level

MARK SCHEME for the October/November 2014 series

4040 STATISTICS

4040/22

Paper 2, maximum raw mark 100

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2014 series for most Cambridge IGCSE[®], Cambridge International A and AS Level components and some Cambridge O Level components.

® IGCSE is the registered trademark of Cambridge International Examinations.

Page 2	Mark Scheme	Syllabus	Paper
	Cambridge O Level – October/November 2014	4040	22

1	(i)	A variable whose outcomes can only take specific values, or can be counted or listed.	B1
	(ii)	Correct example e.g. height, weight...	B1
	(iii)	A variable which has non-numerical outcomes.	B1
	(iv)	Correct example e.g. shoe size, number of people on a bus...	B1
2	(i)	6	B1
	(ii)	15 th value or $(29 + 1)/2$ 5 www	M1 A1
	(iii)	Any attempt to work with a cumulative frequency of 18 or sight of total of 35 $(29 + n + 1)/2 = 18$ $n = 6$ S. C. B1 ^h for 0 following an answer of 4.5 in (ii)	M1 A1
3	(i) (a)	$5/20 \times 4/19$ $(n/m \times (n - 1)/(m - 1))$ or $5/20 \times$ any probability 1/19 oe or 0.053 or better	M1 A1
	(b)	$(5/20 \times 15/19) \times 2$ Product of two probabilities $\times 2$ oe or $(5/20 \times 15/19)$ oe 15/38 oe or 0.39 or better	M1 A1
	(ii)	$8/20 + 12/20 \times 8/20$ $p/m + (m - p)/m \times p/m$ oe (accept additional terms for this mark) 16/25 or 0.64	M1 A1
4	(i)	Median IQR The data contains extreme values (if these are specified they must be the large values of m) or data is not symmetrical. (There must be a single/the same reason.) (B3 for 2 correct measures and correct single/the same reason B2 at least 1 correct measure and correct reason for that measure B1 for median and IQR with incorrect reason or error in reasoning)	B3
	(ii)	$100/150 \times 19$ oe (or accept $50/150 \times 19$ oe) $100/150 \times 19 + 12$ only oe 25	M1 M1 A1

Page 3	Mark Scheme	Syllabus	Paper
	Cambridge O Level – October/November 2014	4040	22

5	(i)	Percentage sectional/component/composite bar chart	B1
	(ii)	42 36 22 36 24 60	B1 B1
	(iii)	Scale from 0, going up in equal intervals to at least their max freq with label 'no. of students' or 'frequency' (may appear in title) Three pairs of bars and correct labelling on horizontal axis Bars correctly shaded and drawn to correct heights (ft their (ii))	B1 B1 B1
	(iv)	'It shows actual numbers/original data, (rather than percentages)' or 'It allows for easy comparison of numbers of males and females (taking each option)'.	B1
6	(i) (a)	A and B, A and C, A and D (–1 each error or omission)	B2
	(b)	B and C, C and D (–1 each error or omission)	B2
	(ii)	EITHER 1/6 (awrt 0.17) and 1/2(oe) seen $P(A \cup B) = P(A) + P(B) - P(A \cap B)$ and $P(A \cap B) = P(A) \times P(B)$ oe 7/12 oe (or awrt 0.58)	B1 M1 A1
		OR Find that there are 21 outcomes in $A \cup B$ Find that there are 36 outcomes in total 7/12 oe (or awrt 0.58)	M1 M1 A1
	(iii)	0 and 5/6 (awrt 0.83)	B1

Page 4	Mark Scheme	Syllabus	Paper
	Cambridge O Level – October/November 2014	4040	22

7	(a) (i)	Two from: To smooth out/eliminate the variation To look for the trend To find seasonal components To make predictions	B1 B1
	(ii)	3	B1
	(iii)	As n is odd (must fit their n) Moving average values correspond to original data points (must fit their n) No (dependent on one M)	M1 M1 A1 [✓]
	(b) (i)	a = 75 b = 70.75 c = 82	B1 B1 B1
	(ii)	62 – 71.5 (= –9.5) or 58 – 67.75 (= –9.75) (ignore sign errors) (sum of two differences)/2 –9.6 (accept –9.63 or –9.625 or –9600 tonnes etc.)	M1 M1 A1
	(iii)	Correctly plotted points Suitable trend line	B1 [✓] B1 [✓]
	(iv)	Attempt at a reading from trend line (even if in wrong place) + ‘their (ii)’ Ans in range 53.9 to 55 (or 53 900 to 55 000) www	M1 A1
8	(i)	Electricity = 0.09 × 5000 or 450 Wages = 6.5 × 4000 or 26 000 15 600 : 450 : 26 000 is equivalent to given ratio (÷ 50)	M1 M1 A1(AG)
	(ii)	100s in first column Ingredients for 2012: 108 Electricity for 2012: 0.11/0.09 × 100 or 0.02/0.09 × 100 122 (allow 122.2 or 122.2...) Wages for 2012: 97	B1 B1 M1 A1 B1
	(iii)	(312 × ‘108’ + 9 × ‘122’ + 520 × ‘97’) Sum of 3 products / (312 + 9 + 520) 101.3 (or 101.4 from 122.2...) (must be 1 dp)	M1 M1 A1 [✓]
	(iv)	(15 600 + ‘450’ + ‘26 000’) × (‘101.3’ / 100) 42 600 (must be 3sf)	M1* M1dep A1 [✓]
	(v)	Two from: Amount of electricity used may have changed Number of staff/hours may have changed Amount of ingredients may have changed Weights/quantities may have changed There may be other expenses/an additional category is suggested	B1 B1

Page 5	Mark Scheme	Syllabus	Paper
	Cambridge O Level – October/November 2014	4040	22

- 9 (i) (a) $1/4$ or $(1/2 \times 1/2)$ seen B1
 $1/4 \times 1/4 \times 1/4$ or $(1/2 \times 1/2) \times (1/2 \times 1/2) \times (1/2 \times 1/2) = 1/64$ B1(AG)
(working essential)
- (b) Evidence that this can happen in three ways: 110, 101, 011 or $3 \times$ M1
 $1/4 \times 1/4 \times 3/4$ M1
 $9/64$ (accept 0.14 here) A1
- OR
9 ways listed HH HH HT, HH HH TH, HH HH TT, HH HT HH, HH TH HH, HH
TT HH, HT HH HH, TH HH HH, TT HH HH or $9 \times$ M1*
 $1/4 \times 1/4 \times 1/4$ M1dep*
- (ii) $P(0 \text{ points}) = 3/4 \times 3/4 \times 3/4$ M1
 $P(1 \text{ point}) = 3 \times 1/4 \times 3/4 \times 3/4$ A1
one correct method B1
 $27/64$ and $27/64$ both correct (accept 0.42 here) B1
Table with $X = 0, 1, 2, 3$
Their probabilities sum to 1
- (iii) $58 \times '1/64'$ M1*
 $+ x \times 'their (i)(b)' = 4$ M1dep
22 A1
- OR
if profit used i.e. \$4 subtracted from winnings then
 $54 \times '1/64' + -4 \times '27/64' + -4 \times '27/64' + (x - 4) \times '9/64' = 0$ M2
- OR
 $54 \times '1/64' + -4 \times '27/64' + -4 \times '27/64' + y \times '9/64' = 0$ M1*
 $y + 4$ M1dep
- (iv) $1/5$ (oe) seen B1
 $50 \times 'their 1/5' + 12.5 \times (1 - 'their 1/5')$ M1
\$20 A1
Correct decision based on 'their (iii)' and 'their \$20' A1✓
- OR
 $1/5$ (oe) seen B1
 $(50 - '22') \times '1/5' + (12.5 - '22') \times (1 - '1/5')$ M1
- \$2 A1
Correct decision based on -ve or +ve result A1✓

Page 6	Mark Scheme	Syllabus	Paper
	Cambridge O Level – October/November 2014	4040	22

- 10 (a) (i)** $(0 \times 13) + 1 \times 11 + 2 \times 7 + 3 \times 6 + 4 \times 4 + 5 \times 1$ M1
64 A1
- (ii)** Total days = $13 + 11 + 7 + 6 + 4 + 1 (=42)$ M1*
'64'/'42' M1dep
1.5 (allow 1.52 or 1.524) A1
- (b)**
- | | | |
|-----|-----|----|
| 10 | 3 | |
| 5.5 | 1.5 | |
| 58 | 15 | |
| 11 | 3 | B4 |
- (B4 for 8 correct, B3 for 6/7 correct, B2 for 4/5 correct, B1 for 2/3 correct)
- (c) (i)** Marks in Algebra generally higher (oe) B1
Marks in Algebra generally more varied (oe) B1
- (ii)** Better in Geometry together with a comparison of her mark with the class mean in terms of the class standard deviation for at least one of Algebra or Geometry. M1
- Correct comparison for both e.g. 1 standard deviation above the mean in Algebra and 2 standard deviations above the mean in Geometry (may be seen as a calculation of standardised scores) A1
- (iii)** $(\pm) \frac{87 - 55}{10}$ or $(\pm) \frac{100 - 60}{\sigma}$ M1
 $\frac{87 - 55}{10} = \frac{100 - 60}{\sigma}$ M1
 $\sigma = 12.5$ A1

Page 7	Mark Scheme	Syllabus	Paper
	Cambridge O Level – October/November 2014	4040	22

11 (i)	47 00 51 32 85 11 67 05 10 (–1 each independent error)	B2
(ii)	01 followed by numbers at equal intervals (not nec ints of 10) 11 21 31 41 51 61 71 81 Intervals of 10 (even if insufficient values or values out of range) 9 values at intervals of 10 all in range (wrap around if necessary)	B1 B1 B1
(iii)	Attempt at machine totals (20, 30, 40) 2 3 4	M1 A1
(iv)	Asad's sample over represents A (or under represents B or C) Or Asad's sample does not accurately represent the jars as he has 4 from machine A (or 2 from machine B or 3 from machine C) Omar's sample accurately represents jars filled by each machine	B1 B1
(v)	44 03 59 14 27 20 78 60 81 (–1 each independent error)	B3
(vi)	39/10 or 51/10 4 and 5	M1 A1
(vii)	Because the mass of jam (in each jar) is being checked A sample stratified by machine is more appropriate	M1 A1